



## Problem 9. «2021-bit key»

A pseudo-random generator produces sequences of bits (that is of 0 and 1) step by step. To start the generator, one needs to pay 1 *nsucoin* and the generator produces a random bit (that is a sequence of length 1). Then, given a generated sequence  $S$  of length  $\ell$ ,  $\ell \geq 1$ , one of the following operations can be applied on each step:

1. A random sequence of 4 bits is added to  $S$ , so a new sequence  $S'$  has length  $\ell + 4$ . The charge for using this operation is 2 *nsucoins*.
2. A random sequence of  $2\ell$  bits is added to  $S$ , so a new sequence  $S'$  has length  $3\ell$ . The charge for using this operation is 5 *nsucoins*.

Bob needs to generate a secret key of length exactly 2021 bits for his new cipher. What is the minimal number of *nsucoins* that he has to pay for the key?

